

STAT 201 Chapter 8.3 & 9.3

Interval & Testing for Mean

# Recall Means Sampling Distributions

- The mean of the sampling distribution for a sample mean will always equal the population mean  $\mu_{\bar{x}} = \mu_x$
- The standard error, the standard deviation of the sample mean, is:

$$\sigma_{\bar{x}} = \frac{\sigma_x}{\sqrt{n}}$$

# Confidence Intervals

- Often, we do not know the population mean
- We use our sample means to make inference on the population parameter
- We **MUST** make sure that the data is obtained through randomization and that distribution of the data is approximately normal
  - For this we require  $n > 30$
  - Otherwise, we can make a graph to confirm

# Confidence Intervals When We Know $\sigma$

- We use our sample means to make interval inference on the population mean

$$\bar{x} \pm z_{\frac{\alpha}{2}} \left( \frac{\sigma}{\sqrt{n}} \right)$$

- $\bar{x}$  is our **point-estimate** for the population proportion
- $z_{\frac{\alpha}{2}} \left( \frac{\sigma}{\sqrt{n}} \right)$  is our **margin of error**

# Confidence Intervals Bounds When We Know $\sigma$

$$\bar{x} \pm z_{\frac{\alpha}{2}} \left( \frac{\sigma}{\sqrt{n}} \right)$$

$$\text{Lower Bound} = \bar{x} - z_{\frac{\alpha}{2}} \left( \frac{\sigma}{\sqrt{n}} \right)$$

$$\text{Upper Bound} = \bar{x} + z_{\frac{\alpha}{2}} \left( \frac{\sigma}{\sqrt{n}} \right)$$

# Confidence Intervals: Margin of Error When We Know $\sigma$

- $z_{\frac{\alpha}{2}} \left( \frac{\sigma}{\sqrt{n}} \right)$  is our **margin of error**
  - **As  $n$  increases**,  $\left( \frac{\sigma}{\sqrt{n}} \right)$  decreases, causing the margin of error to decrease causing the width of the confidence interval to narrow
  - **As  $n$  decreases**,  $\left( \frac{\sigma}{\sqrt{n}} \right)$  increases, causing the margin of error to increase causing the width of the confidence interval to widen

# Confidence Intervals: Margin of Error When We Know $\sigma$

- $z_{\frac{\alpha}{2}} \left( \frac{\sigma}{\sqrt{n}} \right)$  is our **margin of error**
  - **As the confidence level  $\alpha$  decreases**,  $z$  decreases causing the margin of error to decrease, causing the width of the confidence interval to narrow
  - **As the confidence level  $\alpha$  increases**,  $z$  increases causing the margin of error to increase, causing the width of the confidence interval to grow wider

# What if We do not know $\sigma$

- Can we find something to replace  $\sigma$  in  $z_{\frac{\alpha}{2}} \left( \frac{\sigma}{\sqrt{n}} \right)$ ?
- Yes! We can use the sample standard deviation  $s$  to “replace”  $\sigma$ . However, we might lose some “information” or “freedom”
- Recall  $s = \sqrt{Variance} = \sqrt{\frac{\sum(x-\bar{x})^2}{n-1}}$



# Representing Information: Degree of Freedom

- Originally, we know  $\sigma$  and we have  $n$  observations. So we have  $n$  information to use to find the interval; or we can say we have  $n$  “degree of freedom” (free data)
- Now, since we do not know  $\sigma$ , we first use  $n$  observations to estimate the sample standard deviation,  $s$ . So we lose “1” information for the estimation  $s$ , so that we have only  $n-1$  “degree of freedom”. We lose 1 “degree of freedom” by estimating unknown  $\sigma$ .

# Confidence Intervals When We Don't Know $\sigma$

- We use our sample means to make inference on the population mean

$$\bar{x} \pm t_{\frac{\alpha}{2}, n-1} \left( \frac{s}{\sqrt{n}} \right)$$

- $\bar{x}$  is our **point-estimate** for the population proportion
- $t_{\frac{\alpha}{2}, n-1} \left( \frac{s}{\sqrt{n}} \right)$  is our **margin of error**

# Confidence Intervals Bounds When We Don't Know $\sigma$

$$\bar{x} \pm t_{\frac{\alpha}{2}, n-1} \left( \frac{s}{\sqrt{n}} \right)$$

$$\text{Lower Bound} = \bar{x} - t_{\frac{\alpha}{2}, n-1} \left( \frac{s}{\sqrt{n}} \right)$$

$$\text{Upper Bound} = \bar{x} + t_{\frac{\alpha}{2}, n-1} \left( \frac{s}{\sqrt{n}} \right)$$

# Confidence Intervals: Margin of Error When We Don't Know $\sigma$

- $t_{\frac{\alpha}{2}, n-1} \left( \frac{s}{\sqrt{n}} \right)$  is our **margin of error**
  - **As n increases**, t decreases and  $\left( \frac{s}{\sqrt{n}} \right)$  decreases, causing the margin of error to decrease causing the width of the confidence interval to narrow
  - **As n decreases**, t increases and  $\left( \frac{s}{\sqrt{n}} \right)$  increases, causing the margin of error to increase causing the width of the confidence interval to widen

# Confidence Intervals: Margin of Error When We Don't Know $\sigma$

- $t_{\frac{\alpha}{2}, n-1} \left( \frac{s}{\sqrt{n}} \right)$  is our **margin of error**
  - **As the confidence level  $\alpha$  decreases**,  $t$  decreases causing the margin of error to decrease, causing the width of the confidence interval to narrow
  - **As the confidence level  $\alpha$  increases**,  $t$  increases causing the margin of error to increase, causing the width of the confidence interval to grow wider

# Finding t for Our Confidence Intervals

- Say we were trying to find the t-value for a 95% confidence with  $n=10$
- This means  $\alpha = 1 - .95 = .05$  and the degrees of freedom  $= 10 - 1 = 9$
- $t = 2.262$

cum. prob	$t_{.50}$	$t_{.75}$	$t_{.80}$	$t_{.85}$	$t_{.90}$	$t_{.95}$	$t_{.975}$	$t_{.99}$	$t_{.995}$	$t_{.999}$	$t_{.9995}$
one-tail	0.50	0.25	0.20	0.15	0.10	0.05	0.025	0.01	0.005	0.001	0.0005
two-tails	1.00	0.50	0.40	0.30	0.20	0.10	0.05	0.02	0.01	0.002	0.001
df											
1	0.000	1.000	1.376	1.963	3.078	6.314	12.71	31.82	63.66	318.31	636.62
2	0.000	0.816	1.061	1.386	1.886	2.920	4.303	6.965	9.925	22.327	31.599
3	0.000	0.765	0.978	1.250	1.638	2.353	3.182	4.541	5.841	10.215	12.924
4	0.000	0.741	0.941	1.190	1.533	2.132	2.776	3.747	4.604	7.173	8.610
5	0.000	0.727	0.920	1.156	1.476	2.015	2.571	3.365	4.032	5.893	6.869
6	0.000	0.718	0.906	1.134	1.440	1.943	2.447	3.143	3.707	5.208	5.959
7	0.000	0.711	0.896	1.119	1.415	1.895	2.365	2.998	3.499	4.785	5.408
8	0.000	0.706	0.889	1.108	1.397	1.860	2.306	2.896	3.355	4.501	5.041
<b>A</b> 9	0.000	0.703	0.883	1.100	1.383	1.833	2.262	2.821	3.250	4.297	4.781
10	0.000	0.700	0.879	1.093	1.372	1.812	2.228	2.764	3.169	4.144	4.587

# Zoom In

cum. prob	$t_{.50}$	$t_{.75}$	$t_{.80}$	$t_{.85}$	$t_{.90}$	$t_{.95}$	$t_{.975}$	$t_{.99}$	$t_{.995}$	$t_{.999}$	$t_{.9995}$
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- A is the degrees of freedom,  $n-1$
- B is the significance level – for confidence intervals we look for  $\alpha$  in the two-tail row
- C is the t-value associated with the provided degrees of freedom and significance level

# Finding t for Our Confidence Intervals

- Say we were trying to find the t-value for a 99% confidence with  $n=9$
- This means  $\alpha = 1 - .99 = .01$  and the degrees of freedom =  $9 - 1 = 8$
- $t = 3.355$

cum. prob	$t_{.50}$	$t_{.75}$	$t_{.80}$	$t_{.85}$	$t_{.90}$	$t_{.95}$	$t_{.975}$	$t_{.99}$	$t_{.995}$	$t_{.999}$	$t_{.9995}$
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# Finding t for Our Confidence Intervals

- Say we were trying to find the t-value for a 90% confidence with  $n=11$
- This means  $\alpha = 1 - .90 = .10$  and the degrees of freedom =  $11 - 1 = 10$
- $t = 1.812$

cum. prob	$t_{.50}$	$t_{.75}$	$t_{.80}$	$t_{.85}$	$t_{.90}$	$t_{.95}$	$t_{.975}$	$t_{.99}$	$t_{.995}$	$t_{.999}$	$t_{.9995}$
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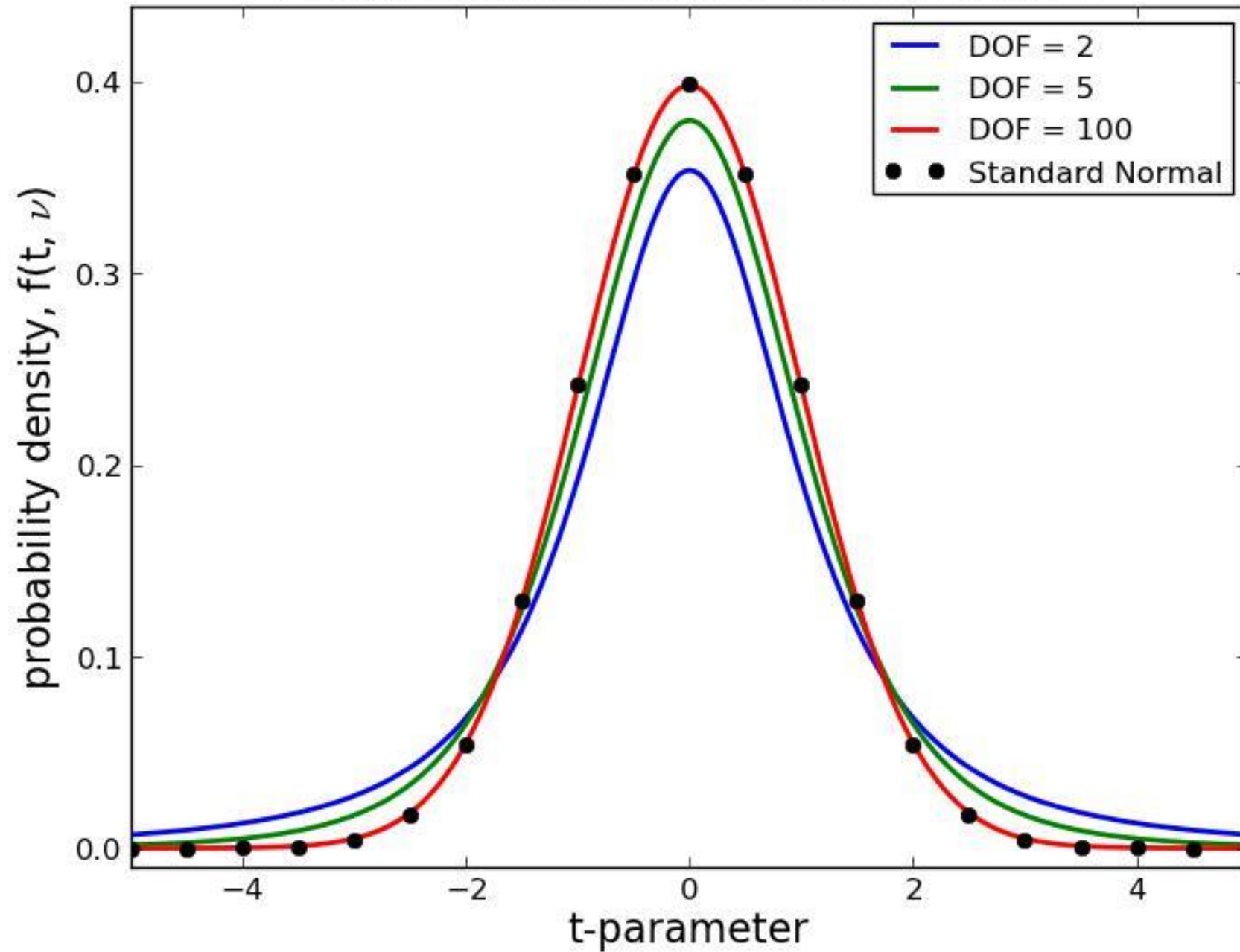
- A is the degrees of freedom,  $n-1$
- B is the significance level – for confidence intervals we look for  $\alpha$  in the two-tail row
- C is the t-value associated with the provided degrees of freedom and significance level

# Properties of the t-distribution

1. The t-distribution is different for different degrees of freedom
2. The t-distribution is centered and symmetric at 0
3. The area under the curve is 1 and  $\frac{1}{2}$  on either side of 0
4. The density (curve) approaches 0 as we move away from 0
5. The t-distribution has fatter tails than the standard normal
6. As the sample size increases t gets close to z

Red properties are the same for normal distribution.

Student distribution for various  $\nu$



# Example

- Suppose a random sample of 81 students from the University of South Carolina was taken. Among the sampled students the sample mean, number of times they inappropriately used the word “like” in a five minute conversation, was 13 times with a **sample standard deviation** of 2.
- Our sample mean =  $\bar{x} = 13$
- Our sample standard deviation =  $s = 2$

# Example

- Our sample mean =  $\bar{x} = 13$
- Our sample standard deviation =  $s = 2$
- Check Assumptions
  - $n > 30$  so it is safe to assume the distribution of  $\bar{x}$  is bell-shaped
  - The data is from a random sample

# Example

- Our sample mean =  $\bar{x} = 13$
- Our sample standard deviation =  $s = 2$
- 95% Confidence Interval for population mean:

$$\bar{x} \pm t_{\frac{.05}{2}, 80} \left( \frac{s}{\sqrt{n}} \right)$$
$$= (11.5578, 14.4422)$$



# Example

(11.5578, 14.4422)

- We are 95% confident that the true population mean of number of times a University of South Carolina student inappropriately says “like” in a five minute conversation is between 11.5578 and 14.4422 times, or more specifically between 12 and 14 times.

# Example

- What if I do not tell you the sample mean is 13 and sample standard deviation 2, instead give you the original data, do you know what to do?
- This time, you need to calculate the sample mean  $\bar{x}$  and sample standard deviation  $s$  using Statcrunch, then use the interval formula to find the confidence interval.

## Example 2

- Suppose a random sample of 20 kids was chosen in a fat camp. Among the sampled kids we saw a bell-shaped distribution with a sample mean of number of pounds lost was 2 and a population standard deviation of 4.
- Our sample mean =  $\bar{x} = 2$
- Our population standard deviation =  $\sigma = 4$

# Example 2

- Check Assumptions
  - **N<30 BUT** we were told it is safe to assume the data was bell-shaped which indicates the distribution of  $\bar{x}$  is bell-shaped
  - The data is from a random sample

## Example 2

- 90% Confidence Interval for population mean number of pounds lost at fat camp was:

$$\begin{aligned} & \bar{x} \pm z_{.90} \left( \frac{\sigma}{\sqrt{20}} \right) \\ &= 2 \pm (1.64) \left( \frac{4}{\sqrt{20}} \right) \\ & \quad (.5331, 3.4669) \end{aligned}$$

## Example 2

$(.5331, 3.4669)$

- We are 90% confident that the true population mean number of pounds lost at fat camp per kid is between .5331 and 3.4669 pounds.

# From Confidence Intervals to Testing

- As we see in the last example we can come up with interesting observations of our confidence intervals
- Next we will learn how to formally test whether or not the population mean is a particular value based off our sample mean (without knowing standard deviation  $\sigma$ )

# Hypothesis Test for Means: Step 1

- State Hypotheses:
  - **Null hypothesis:** that the population mean equals some  $\mu_o$ 
    - $H_o: \mu \leq \mu_o$  (one sided test)
    - $H_o: \mu \geq \mu_o$  (one sided test)
    - $H_o: \mu = \mu_o$  (two sided test)
  - **Alternative hypothesis:** What we're interested in
    - $H_a: \mu > \mu_o$  (one sided test)
    - $H_a: \mu < \mu_o$  (one sided test)
    - $H_a: \mu \neq \mu_o$  (two sided test)



# Hypothesis Test for Means: Step 2

- Check the assumptions
  - The variable must be quantitative
  - The data are obtained using randomization
  - We're dealing with data from the normal distribution
    - If  $n > 30$
    - If a histogram of the data is approximately normal

# Hypothesis Test for Means: Step 3

- Calculate Test Statistic,  $t^*$ 
  - The test statistic measures how different the sample mean we have is from the null hypothesis
  - We calculate the t-statistic by assuming that  $\mu_0$  is the population mean

$$t = \frac{(\bar{x} - \mu_0)}{\frac{s}{\sqrt{n}}}$$

# Hypothesis Test for Means: Step 4

- Determine the P-value
  - The P-value describes how unusual the data would be if  $H_0$  were true.
  - We will use software to find this

# Hypothesis Test for Means: Step 4

- Determine the P-value
  - The P-value describes how unusual the sample data would be if  $H_o$  were true.
  - Again, we will use software or your calculator to find this, or I will give it to you.

Alternative Hypothesis	Probability	Formula for the P-value
$H_a: p > p_o$	Right tail	$P(T > t)$
$H_a: p < p_o$	Left tail	$P(T < t)$
$H_a: p \neq p_o$	Two-tail	$2 * P(T < - t )$

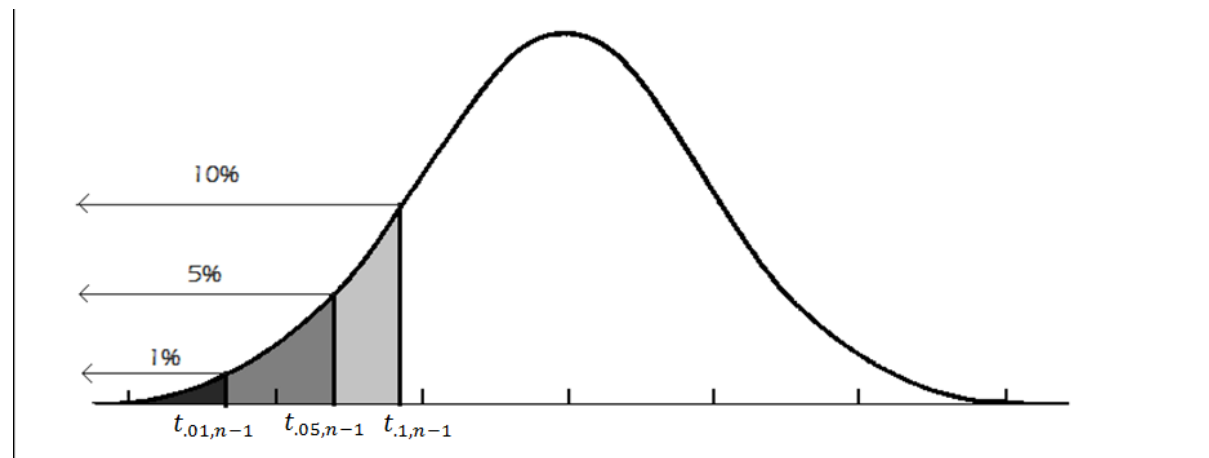
# Hypothesis Test for Means: Step 5

- Summarize the test by reporting and interpreting the P-value
  - Smaller p-values give stronger evidence against  $H_o$
- If  $\text{p-value} \leq (1 - \text{confidence}) = \alpha$ 
  - Reject  $H_o$ , with a p-value = \_\_\_\_\_, we have sufficient evidence that the alternative hypothesis might be true
- If  $\text{p-value} > (1 - \text{confidence}) = \alpha$ 
  - Fail to reject  $H_o$ , with a p-value = \_\_\_\_\_, we do not have sufficient evidence that the alternative hypothesis might be true

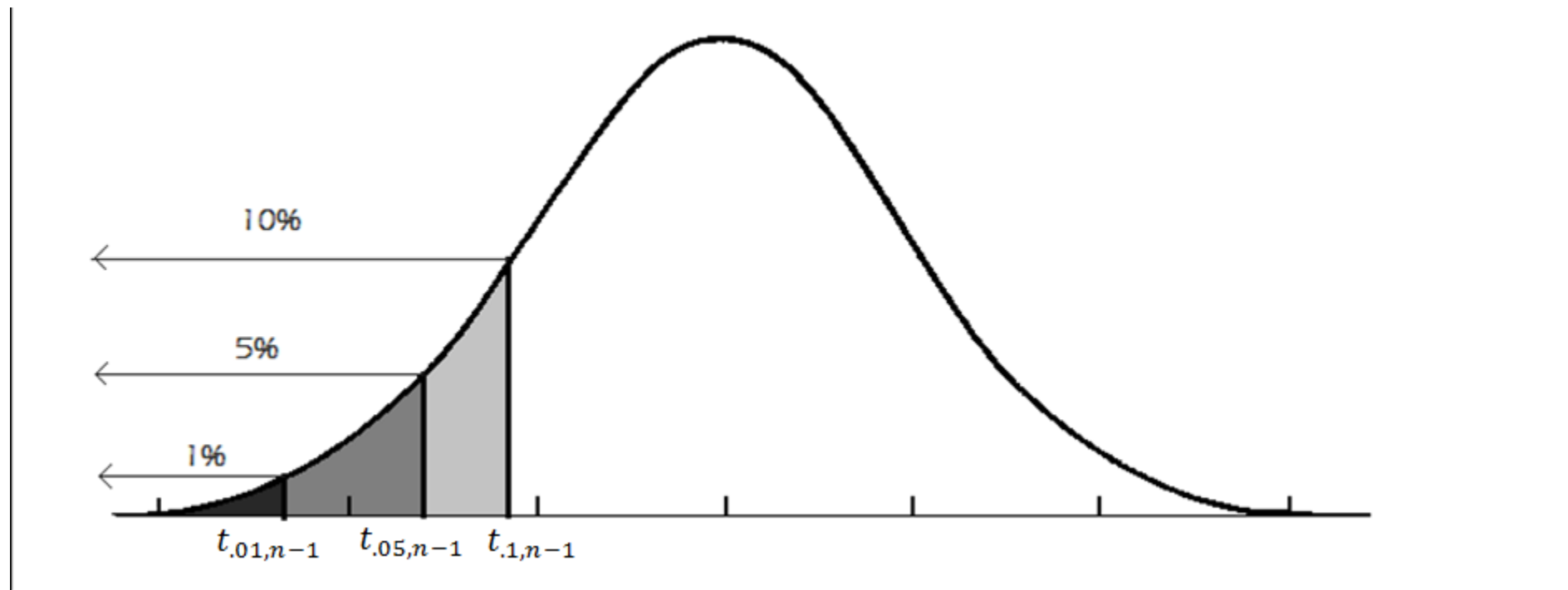
# Hypothesis Test for Means– Step Five with Pictures

- For a left tailed test:  $H_a: \mu < \mu_o \rightarrow$  We have rejection regions for  $H_o$  are as follows

Confidence	Reject (test stat)	Reject (p-value)
0.90	Test-stat $< -t_{.10,n-1}$	P-value $< .1$
0.95	Test-stat $< -t_{.05,n-1}$	P-value $< .05$
0.99	Test-stat $< -t_{.01,n-1}$	P-value $< .01$



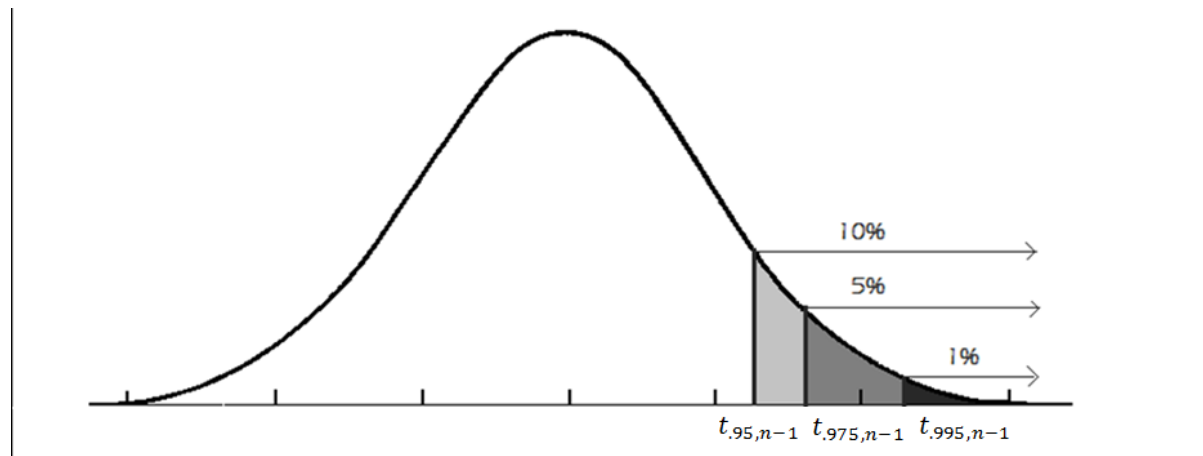
# Zoom In



# Hypothesis Test for Means– Step Five with Pictures

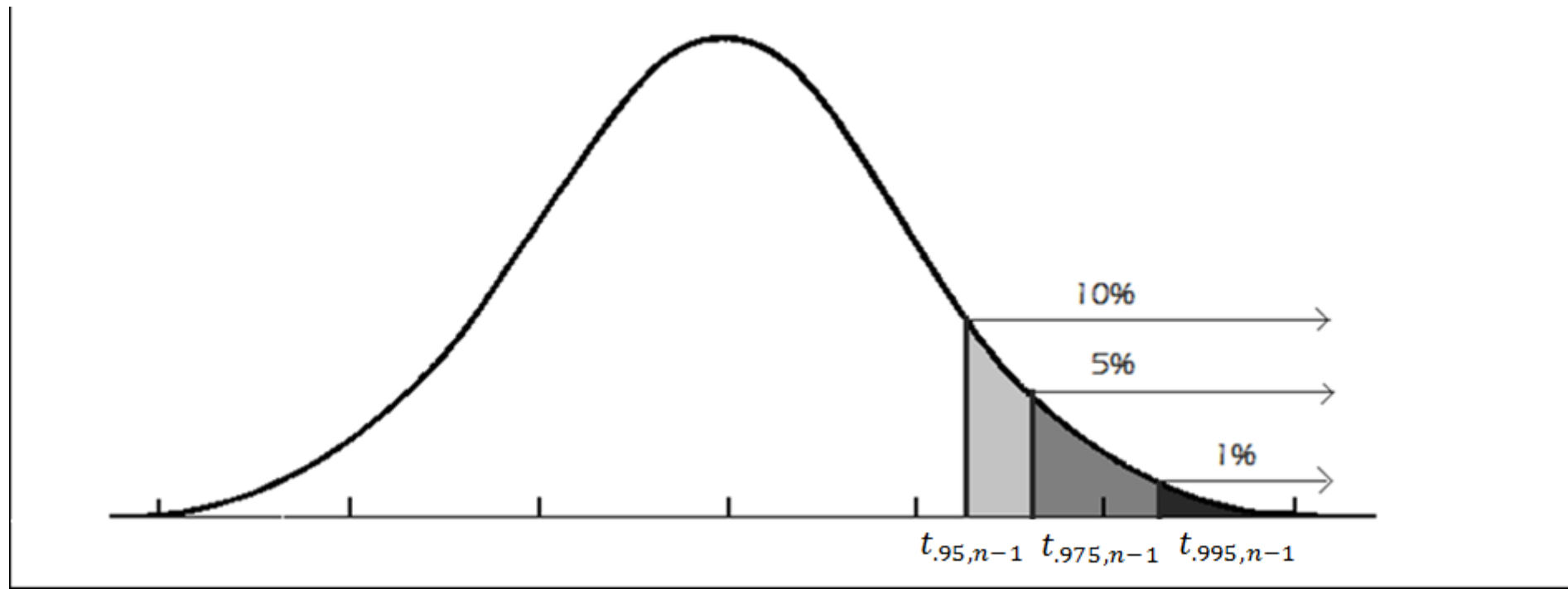
- For a left tailed test:  $H_a: \mu > \mu_o \rightarrow$  We have rejection regions for  $H_o$  are as follows

Confidence	Reject (test stat)	Reject (p-value)
0.90	Test-stat $< -t_{.90,n-1}$	P-value $< .1$
0.95	Test-stat $< -t_{.95,n-1}$	P-value $< .05$
0.99	Test-stat $< -t_{.99,n-1}$	P-value $< .01$





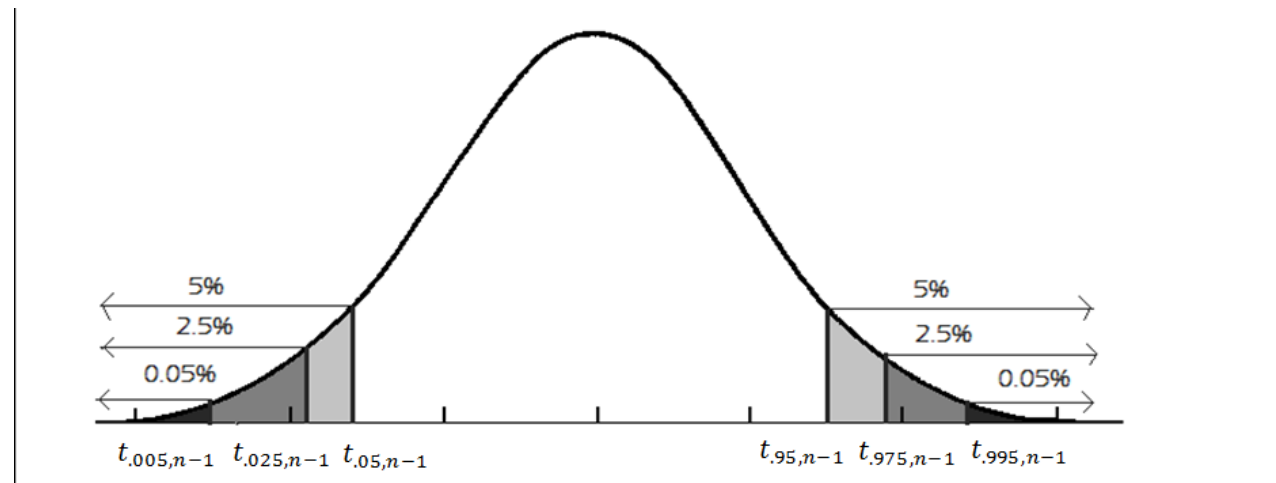
# Zoom In



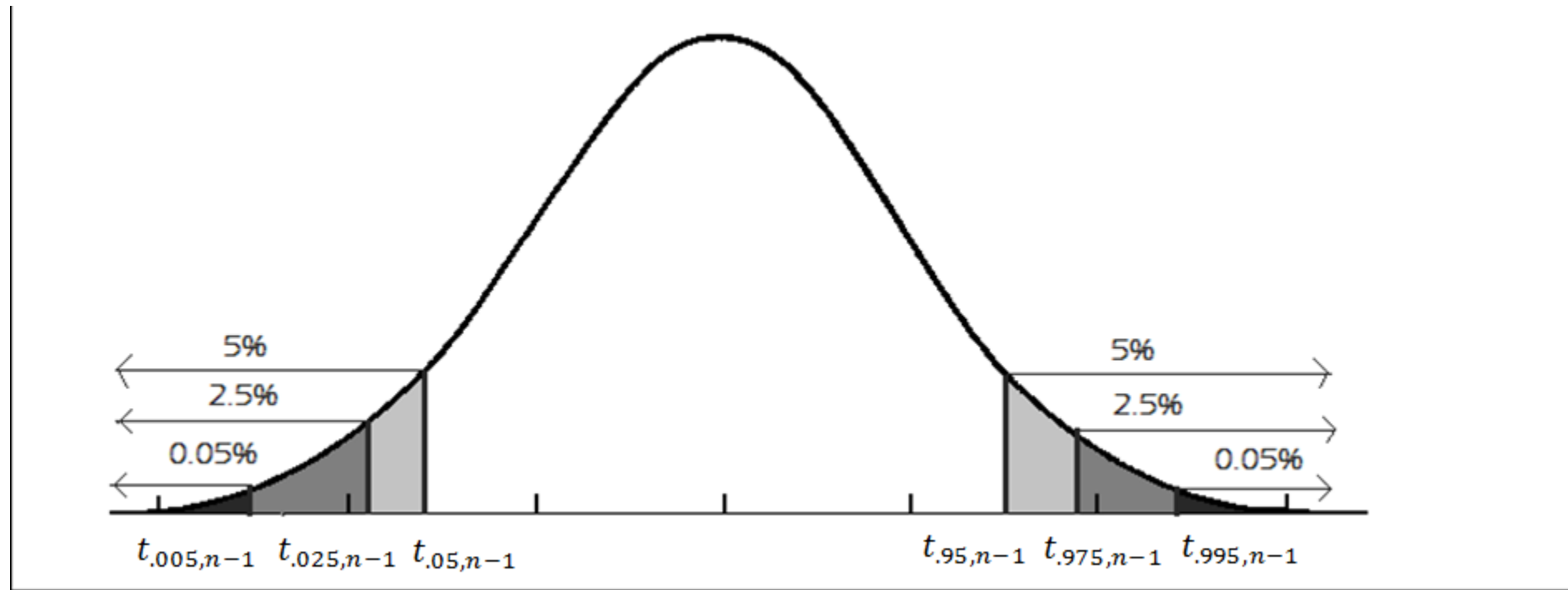
# Hypothesis Test for Means– Step Five with Pictures

- For a two tailed test:  $H_a: \mu \neq \mu_o \rightarrow$  We have rejection regions for  $H_o$  are as follows

Confidence	Reject (test stat)	Reject (p-value)
0.90	$ \text{Test-stat}  < -t_{.90,n-1}$	P-value<.1
0.95	$ \text{Test-stat}  < -t_{.95,n-1}$	P-value<.05
0.99	$ \text{Test-stat}  < -t_{.99,n-1}$	P-value<.01



# Zoom In



# Example 1

- An engineer at Budweiser came up with the idea of selling beers with a new designed machine! He wishes to show that the mean number of ounces bottled by his new machine greater than 4.5oz at a .05 significance level, or 95% confidence.
- A random sample of ten cans produces the data below  
4.5, 5.6, 4.9, 3.8, 4.1, 4.3, 4.4, 4.7, 5.0, 4.6

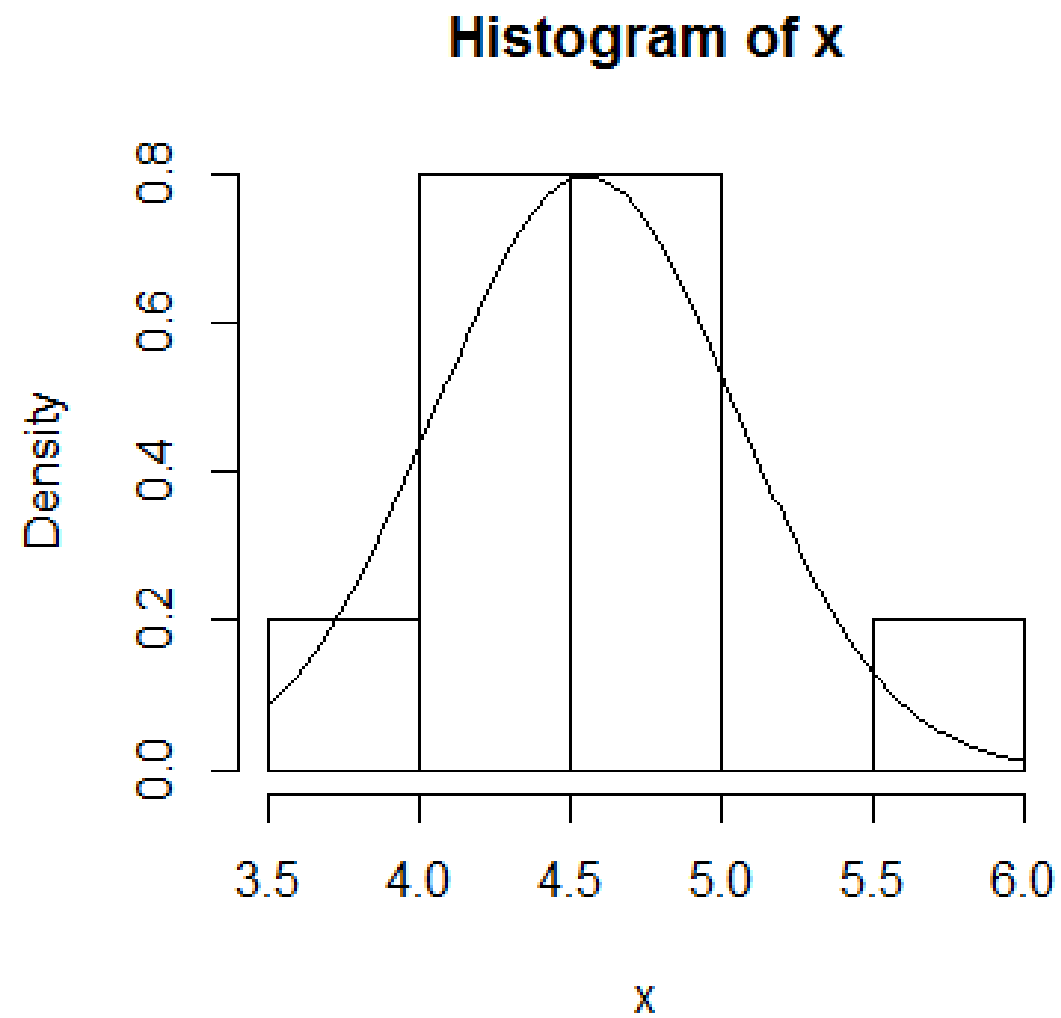
## Example 1 – Step One

- A random sample of ten produces the data below  
4.5, 5.6, 4.9, 3.8, 4.1, 4.3, 4.4, 4.7, 5.0, 4.6
- State the Hypotheses: we are interested in whether or not the mean is **greater than 4.5 oz**
  - $H_o: \mu \leq 4.5$
  - $H_a: \mu > 4.5$

## Example 1 – Step Two

- A random sample of ten produces the data below  
4.5, 5.6, 4.9, 3.8, 4.1, 4.3, 4.4, 4.7, 5.0, 4.6
- Check Assumptions:
  - The data is quantitative
  - The sample is randomly selected
  - Even though  $n < 30$ , a histogram of the data shows approximately normal

Check it!



# Example 1 – Step Three

- Calculate Test Statistic

Variable	Sample Mean ( $\bar{x}$ )	Standard Deviation ( $s_x$ )	Standard Error ( $s_{\bar{x}}$ )
Ounces Filled	4.59	.5043	.1595

$$t^* = \frac{(\bar{x} - \mu_o)}{\frac{s}{\sqrt{n}}} = \frac{4.59 - 4.5}{\frac{.5043}{\sqrt{10}}} = \frac{.09}{.1595} = .5643$$



## Example 1 – Step Four

- Determine P-value

P-value from software is .2932

# Example 1 – Step Five

- State Conclusion

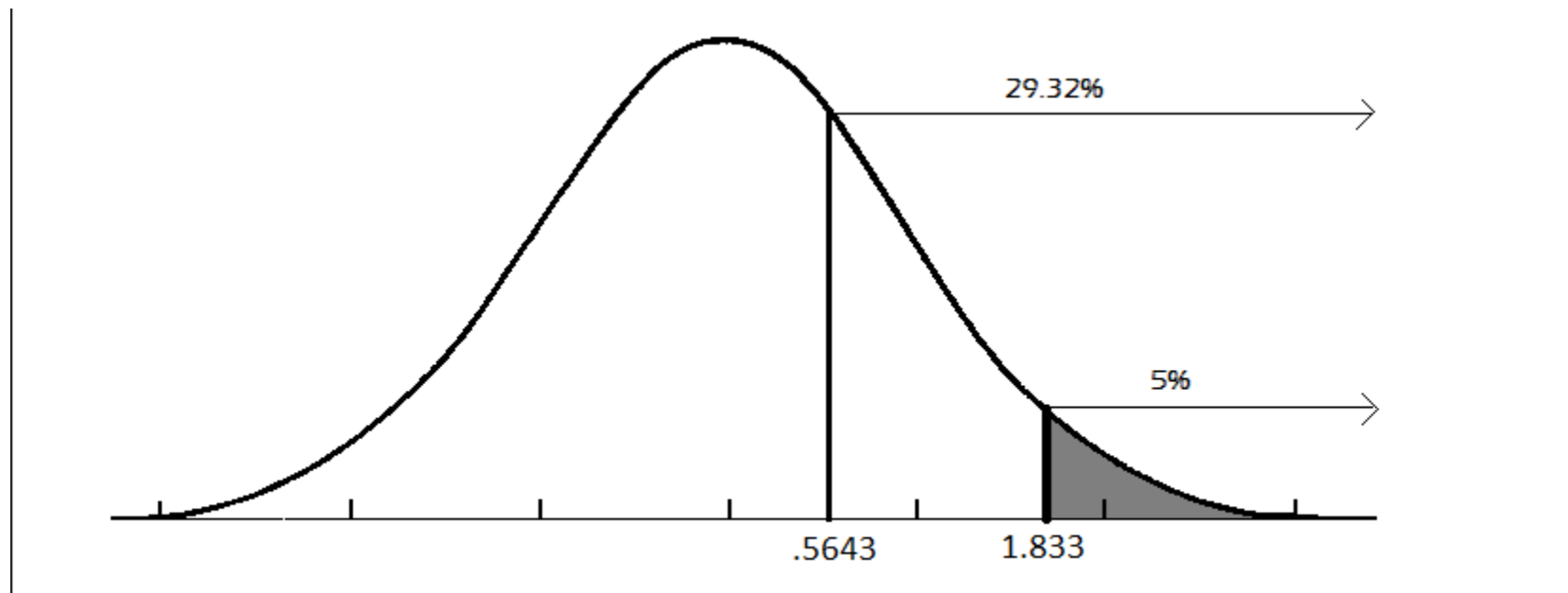
- Since  $.2932 > .05$  we fail to reject  $H_0$

At the .05 level of significance, or 95% confidence level, there isn't sufficient evidence that the mean fill is greater than 4.5 oz

# Example 1 – Step Five with Pictures

- State Conclusion

- Anything with a p-value  $< .05$  or a t-value  $> t_{1-\alpha, n-1} = t_{.95, 9} = 1.833$  will be in the rejection region
- Since  $.2932 > .05$  we fail to reject  $H_0$



# Zoom In

